

# CENTRAL WISCONSIN MATHEMATICS LEAGUE

Meet I

November 8, 2000

Category I (Geometry)

1–10: Multiple Choice (4 points each). On your answer sheet, circle the letter of the one best choice.

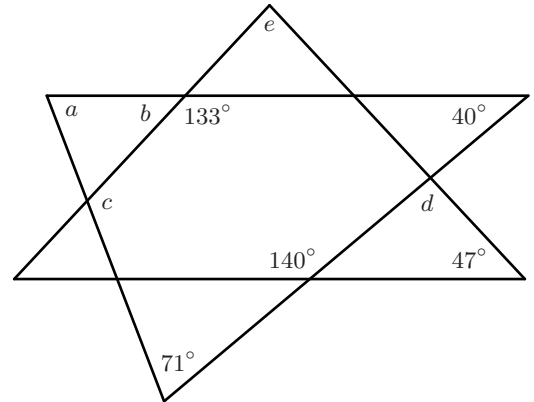
- The statements “if  $a$ , then  $b$ ” and “if  $b$ , then  $a$ ” are
  - contrapositives
  - converses
  - inverses
  - equivalent
  - none of these
- An angle with measure  $111^\circ$  is an example of a(n)
  - acute angle
  - obtuse angle
  - right angle
  - complementary angle
  - supplementary angle
- If a triangle is equilateral, then it has
  - three congruent sides
  - three congruent angles
  - exactly two congruent sides and two congruent angles
  - both (a) and (b)
  - none of these
- If a line  $\ell$  has two different points  $A$  and  $B$  on a plane  $p$ , then we can say
  - $p$  is contained in  $\ell$
  - $\overline{AB}$  is contained in  $p$
  - $\ell$  is contained in  $p$
  - both (a) and (b)
  - both (b) and (c)
- In three-dimensional space, distinct lines  $a$ ,  $b$ , and  $c$  are such that  $a$  is perpendicular to  $b$ , and  $b$  is perpendicular to  $c$ . Which one of the following is impossible?
  - $a$  is parallel to  $c$ .
  - $a$ ,  $b$ , and  $c$  are concurrent.
  - $a$  is not parallel to  $b$ .
  - $a$  is skew to  $c$ .
  - $a$  and  $c$  are parallel to  $b$ .
- A line segment has
  - 0 endpoints
  - 1 endpoint
  - 2 endpoints
  - (a) or (b)
  - none of these
- If two angles are vertical angles, then we know
  - the two angles are congruent
  - the sum of their measures is  $180^\circ$
  - the sum of their measures is  $90^\circ$
  - both angles are right angles
  - both angles are straight angles
- A triangle with three sides of different lengths is
  - obtuse
  - acute
  - isosceles
  - equilateral
  - scalene
- If line segments  $\overline{AB}$  and  $\overline{CD}$  are congruent to each other, we may conclude that
  - the segments are perpendicular
  - the segments are parallel
  - the segments have equal length
  - $A = C$  and  $B = D$
  - both (b) and (c)
- The geometric symbol for *congruent* is
  - $\sim$
  - $\cong$
  - $\approx$
  - $=$
  - $\perp$

11–16: *Miscellaneous Problems (point values as indicated). On your answer sheet, circle the correct response or write your answer in the blank(s) provided. (P) means that partial credit may be given.*

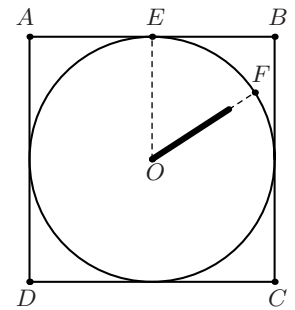
11. [10 points] The measure of the complement of an angle  $X$  is four-ninths the measure of the supplement of  $X$ . Find the *exact* measure of  $X$ .

12. [10 points] How many different lines are determined by five coplanar points, no three of which are collinear?

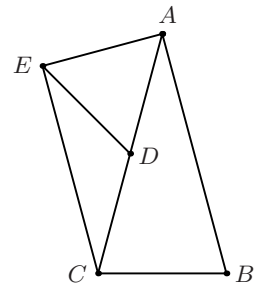
13. [10 points](P) Use the information in the given figure to find the *exact* angle measures  $a$ ,  $b$ ,  $c$ ,  $d$ , and  $e$ .



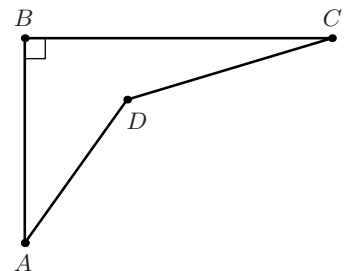
14. [10 points] The face of a clock consists of a circle with radius  $r$  and center  $O$  which is inscribed in square  $ABCD$ . Let  $E$  be the midpoint of  $\overline{AB}$  and let  $F$  be the point on the circle which corresponds to the tip of the hour hand. To the *nearest minute*, what time does the clock read when the measure of  $\angle EOF$  is  $57^\circ$ ?



15. [10 points] The measures of  $\angle ACB$  and  $\angle ABC$  both equal  $75^\circ$ ,  $D$  is the midpoint of  $\overline{AC}$ , and triangle  $ADE$  is equilateral. Find the *exact* measure of  $\angle DCE$ .



16. [10 points] Point  $D$  lies in the interior of the right angle  $ABC$  such that  $m(\angle BCD) = 17^\circ$  and  $m(\angle CDA) = 129^\circ$ . Find the *exact* measure of  $\angle DAB$ .



Student's Answer Sheet

Name: \_\_\_\_\_  
PRINT: First Last

School: \_\_\_\_\_ Code

Multiple Choice (4 points each). Circle the letter of the one best choice.

1.    **a**        **b**        **c**        **d**        **e**
  
2.    **a**        **b**        **c**        **d**        **e**
  
3.    **a**        **b**        **c**        **d**        **e**
  
4.    **a**        **b**        **c**        **d**        **e**
  
5.    **a**        **b**        **c**        **d**        **e**
  
6.    **a**        **b**        **c**        **d**        **e**
  
7.    **a**        **b**        **c**        **d**        **e**
  
8.    **a**        **b**        **c**        **d**        **e**
  
9.    **a**        **b**        **c**        **d**        **e**
  
10. **a**        **b**        **c**        **d**        **e**

Miscellaneous Problems (point values as indicated). Circle the correct response or write your answer in the blank(s) provided; the boxes at the right are for grading use only. (P) means that partial credit may be given.

11. measure of  $X =$  \_\_\_\_\_<sup>o</sup>

|    |  |
|----|--|
| 10 |  |
|----|--|

12. \_\_\_\_\_ lines      

|    |  |
|----|--|
| 10 |  |
|----|--|

13.  $a =$  \_\_\_\_\_<sup>o</sup>

|     |  |
|-----|--|
| 10P |  |
|-----|--|

$b =$  \_\_\_\_\_<sup>o</sup>

$c =$  \_\_\_\_\_<sup>o</sup>

$d =$  \_\_\_\_\_<sup>o</sup>

$e =$  \_\_\_\_\_<sup>o</sup>

14. clock reads \_\_\_\_\_      

|    |  |
|----|--|
| 10 |  |
|----|--|

15.  $m(\angle DCE) =$  \_\_\_\_\_<sup>o</sup>

|    |  |
|----|--|
| 10 |  |
|----|--|

16.  $m(\angle DAB) =$  \_\_\_\_\_<sup>o</sup>

|    |  |
|----|--|
| 10 |  |
|----|--|

**FOR GRADING USE ONLY**

Mult Choice: \_\_\_\_\_ correct  $\times$  4 = \_\_\_\_\_

Misc Problems: \_\_\_\_\_ total = \_\_\_\_\_

**TOTAL SCORE**